

**KAKARAPARTI BHAVANARAYANA COLLEGE (Autonomous)**  
**Department Of Mathematics**

Programme	Semester:	Title of The Course		Course Code:		W.E.F
B.VOC(IT)& B.VOC(WT)	I	Discrete Mathematics - I		R20ITDM101 & R20WSDM101		2020-21
Total No of Hours for Teaching – Learning		Instructional Hours for Week		Duration of Semester End Examination in Hours		Max Marks
60 Hours		Theory		3 Hours		CIA
		4				SEE
						25
						75
						4

**COURSE OBJECTIVES**

The aim of this course is to provide necessary information to solve problems on Algebra and their applications.

**COURSE OUTCOME**

- Understand the concept of Algebra .
- Finding Solutions in Special products , exponents , Fundamental operations ..
- Applications in classical mechanics.

**UNIT – I : Algebra**

1. Fundamental Operations with number addition, subtraction, multiplication and division of numbers - exponential and powers – laws of exponents – operations with fractional.
2. Fundamental operations with algebraic expressions – differential types of polynomials, degree of a polynomials – addition, multiplication division of algebraic expressions.

**UNIT-II**

1. Special products like  $a^n - b^n$ ,  $a^n + b^n$  etc.
2. Factorising-common monomial factor, difference of two sequences, perfect square binomials, sum of difference of two cubes – grouping of terms – factors of  $a^n + b^n$  addition and subtraction of suitable terms – HCF & LCM of algebraic expressions.

### **UNIT – III**

1. Fractions – the algebraic sum of fractions product of fractions – quotient of two fractions & complex fractions.
2. Exponents – positive fractional exponent negative integral exponent – Rational exponents – general laws of exponents.

### **UNIT - IV**

1. Radicals – Radical form – laws for radicals similar radicals – addition, multiplication & division of radical & conjugates.

### **UNIT-V**

1. Simple operation with complex numbers – imaginary number – squareroot of  $\sqrt{-1}$  complex numbers – algebraic addition, subtraction, multiplication & division of simple complex numbers. Note : Problems only on all the above concepts

### **PRESCRIBED BOOKS**

- Munay R. Spiegel, Robert E. Maver Schaum's outlines series College algebra – 1956 Edition
- Chapters – 1,2,4,5,6,7,8,9 content & treatments as it is

### **Reference Books :**

- Bhavanari Satyanarayana & Kuncham Syam Prasad
- Discrete Mathematics & Graph theory, Printice Hall of India, Learning, New Delhi 2009.

### **Paper Setting:**

- Section A – One Question from each chapter of Unit – IV & Unit - V
  - Two Questions from Unit I , Unit II & Unit III .
- Section B - Two Questions from each Unit.

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**Model Question Paper**

**SECTION-A (Short Answer Questions)**

*(Instructions to the paper setter: Set minimum ONE question from each unit, max Eight from all.)*

**Answer any five of the following questions**

**5x5=25**

1. Evaluate the expression given (i)  $x=2, y=3, a=\frac{1}{2}, b=-\frac{2}{3}, \left(\frac{x}{y}\right)^2 - 3\left(\frac{b}{a}\right)^3$ .

(ii)  $x=2, y=-1, z=3, a=0, b=4, c=\frac{1}{3} \frac{4x^2y(z-1)}{a+b-3c}$ .

2. Find  $(e^y + 1)(e^y - 1)(e^{2y} + 1)(e^{4y} + 1)(e^{8y} + 1)$ .

3. Divide  $x^2+2x^4-3x^3+x-2$  by  $x^2-3x+2$ .

4. Add the algebraic expressions  $2a^2bc-2acb^2+5c^2ab, 4b^2ac+4bca^2-7ac^2b,$   
 $4abc^2-3a^2bc- 3ab^2c, b^2ac-abc^2-3a^2bc$ .

5. (i) Find the L.C.M. of  $9x^4y^2$  and  $12x^3y^3$ .

(ii) Find the G.C.F. of  $48r^3t^4$  and  $54r^2t^6$ .

6. Find the complex fraction of  $1 - \frac{1}{2 - \frac{1}{3 - \frac{2a-1}{2a+1}}}$ .

7. (i) Find the value of  $(0.004)(30000)^2$ .

(ii) Evaluate  $4x^{-2/3} + 3x^{1/3} + 2x^0$  when  $x = 8$ .

8. Perform the indicated operations both algebraically and graphically  $(2+6i) + (5+3i)$ .

**SECTION-B (Essay Questions)**

*(Instructions to the paper setter: Set minimum two questions from each unit, either or internal choice)*

**Answer All of the following questions**

**5x10=50**

9. a) Add the algebraic expressions

(i)  $x^2+y^2-z^2+2xy-2yz, y^2+z^2-x^2+2yz-2zx, z^2+x^2-y^2+2zx-2xy.$

(ii) Perform the division of  $2x^6+5x^4-x^3+1$  by  $-x^2+x+1.$

**Or**

b) Find the product of  $(3y+x) (81y^4-27y^3x+9y^2x3yx^3+x^4)$

10. a) (i) Find the factor of  $(x^2-4z^2+9y^2-6xy)$

(ii) Find the L.C.M. of  $2^3.3^2(x-y)^3 (x+2y)^2, 2^2.3^3(x-y)^2 (x+2y)^3,$

$3^2 (x-y)^2(x+2y)$

**Or**

b) Find the perfect square of  $4m^6n^6+32m^4n^4+64m^2n^2.$

11. a) Find the addition and subtraction of

$$\frac{3x-6}{4x^2+12x+16} \frac{2x-5}{6x^2-6} + \frac{3x^2+3}{8x^2+40x+32}$$

**Or**

b) (i) Find the value of  $4x^{-2/3} + 3x^{1/3} + 2x^0$  when  $x = 8.$

(ii) Find the value of  $(0.125)^{1/3}.0.25^{-1/2}.$

12. a) (i) Find the multiplication of  $(\sqrt{x+y} - z) (\sqrt{x+y} + z)$

(ii) Find  $\frac{1}{5}(-10 + \sqrt{-125})$

**Or**

b) Show that  $\frac{x+\sqrt{y}}{x-\sqrt{y}} + \frac{x-\sqrt{y}}{x+\sqrt{y}} = \frac{2x^2+2y}{x^2-y}$

13. a) Find  $\frac{2\sqrt{3}+2i}{3\sqrt{2}-4\sqrt{3}i}$  Or

b) Find  $\left(\frac{\sqrt{2}}{2} + \frac{\sqrt{2}}{2}i\right)$

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60 Hours		Theory		3 Hours	CIA	SEE	
		4			25	75	4

**QUESTION BANK**

**SHORT ANSWER QUESTIONS :**

**SECTION-A**

1. Evaluate the expression given

(i)  $x=2, y=3, a=1/2, b= -2/3, (x/y)^2 - 3(b/a)^3$ .

(ii)  $x=2, y=-1, z=3, a=0, b=4, c=1/3 \frac{4x^2y(z-1)}{a+b-3c}$ .

2. Find  $(e^y + 1) (e^y - 1) (e^{2y} + 1)(e^{4y} + 1)(e^{8y} + 1)$ .

3. Add the algebraic expression  $x^2+y^2-z^2+2xy-2yz, y^2+z^2-x^2+2yz-2zx,$

$$z^2+x^2-y^2+2zx-2xy$$

4. Add  $7x+3y^3-4xy, 3x-2y^3+7xy, 2xy-5x-6y^3+7xy^3$ .

5. Add the algebraic expression  $2a^2bc-2acb^2+5c^2ab, 4b^2ac+4bca^2-7ac^2b,$   
 $4abc^2-3a^2bc-3ab^2c, b^2ac-abc^2-3a^2bc$

## SECTION-B

6. (i) Find the L.C.M. of  $9x^4y^2$  and  $12x^3y^3$ .

(ii) Find the G.C.F. of  $48r^3t^4$  and  $54r^2t^6$ .

7. Find the value of  $(u-v)^3(u+v)^3$

8. Simplify  $(x^2-x+1)^2(x^2+x+1)^2$

9. Simplify  $(2t^2+s)(3t^2+4s)$

10. Find the value of  $(ab^2+2b)^3$

11. Find the factors of  $6x^2-7x-5$

12. Find the factors of  $3x^2+10x+3$

## SECTION-C

13. Find the complex fraction of  $1 - \frac{1}{2 - \frac{1}{3 - \frac{2a-1}{2a+1}}}$ .

14. (i) Find the value of  $(0.004)(30000)^2$ .

(ii) Evaluate  $4x^{-2/3} + 3x^{1/3} + 2x^0$  when  $x = 8$ .

15. Simplify  $\frac{x^2-3x+2}{2-x}$

16. Show that  $\frac{\frac{x+1}{1} - \frac{x-1}{1}}{\frac{x-1}{1} + \frac{x+1}{1}} = 2$

17. Evaluate  $\frac{-3^2(-2x)^{-3}}{(x+1)^{-2}}$  when  $x=2$ .

18. Evaluate  $(0.004)(30.000)^2$ .

## SECTION-D

19. Find the value of  $\frac{5}{\sqrt[2]{3} + \sqrt{2}}$ .

20. Rationalise the denominator of  $\frac{3}{\sqrt[3]{5}-2}$

21. Simplify  $\frac{3}{\sqrt{5} + \sqrt{2}}$

22. Simplify  $(3\sqrt{2} - 4\sqrt{5})(2\sqrt{3} + 3\sqrt{6})$

23. Find the value of  $(\sqrt{x+y} - z)(\sqrt{x+y} + z)$

24. Find  $\sqrt[12]{8x^3y^6}$ .

## SECTION-E

25. Perform the indicated operations both algebraically and graphically  $(2+6i) + (5+3i)$ .

26. Find  $(5+3i)(2-2i)$

27. Find  $\frac{1+i}{3-i}$

28. Find  $\frac{-1}{2-2i}$

29. Find  $\frac{3-\sqrt{2}i}{\sqrt{2}i}$

30. Find the value of  $\left(\frac{2}{3} - \frac{1}{2}i\right) - \left(\frac{-1}{3} + \frac{1}{2}i\right)$

## LONG ANSWER QUESTIONS :

### SECTION-A

1. Add the algebraic expressions

(i)  $x^2+y^2-z^2+2xy-2yz$ ,  $y^2+z^2-x^2+2yz-2zx$ ,  $z^2+x^2-y^2+2zx-2xy$ .

(ii) Perform the division of  $2x^6+5x^4-x^3+1$  by  $-x^2+x+1$ .

2. Find the product of  $(3y+x)(81y^4-27y^3x+9y^2x^3yx^3+x^4)$

3. Divide  $x^2+2x^4-3x^3+x-2$  by  $x^2-3x+2$

4. Solve  $\frac{16y^4-1}{2y-1}$

### SECTION-B

5. (i) Find the factor of  $(x^2-4z^2+9y^2-6xy)$

(ii) Find the L.C.M. of  $2^3 \cdot 3^2(x-y)^3(x+2y)^2$ ,  $2^2 \cdot 3^3(x-y)^2(x+2y)^3$ ,

$3^2(x-y)^2(x+2y)$

6. Find the perfect square of  $4m^6n^6+32m^4n^4+64m^2n^2$

7. Find the GCF and LCM of  $y^4-16$ ,  $y^2-4$ ,  $y^2-3y+2$ .

8. Find  $(3y+x)(81y^4-27y^3x+9y^2x^2-3yx^3+x^4)$

### SECTION-C

9. Find the addition and subtraction of  $\frac{3x-6}{4x^2+12x+16} - \frac{2x-5}{6x^2-6} + \frac{3x^2+3}{8x^2+40x+32}$

10. (i) Find the value of  $4x^{-2/3} + 3x^{1/3} + 2x^0$  when  $x = 8$ .

(ii) Find the value of  $(0.125)^{1/3} \cdot 0.25^{-1/2}$ .

11. Evaluate  $3 \sqrt{\frac{(0.004)^4(0.0036)}{(120000)^2}}$

12. Find that of  $\frac{(80,000,000)^2(0,000003)}{(6,00,000)(0.002)^4}$

### SECTION-D

13. (i) Find the multiplication of  $(\sqrt{x+y} - z)(\sqrt{x+y} + z)$

(ii) Find  $\frac{1}{5}(-10 + \sqrt{-125})$

14. Show that  $\frac{x+\sqrt{y}}{x-\sqrt{y}} + \frac{x-\sqrt{y}}{x+\sqrt{y}} = \frac{2x^2+2y}{x^2-y}$

15. Simplify  $\frac{x+\sqrt{x}}{1+\sqrt{x}+x}$

16. Find  $\frac{2+\sqrt{3}+\sqrt{5}}{2+\sqrt{3}-\sqrt{5}}$

### SECTION-E

17. Find  $\frac{2\sqrt{3}+2i}{3\sqrt{2}-4\sqrt{3}i}$

18. Find  $\left(\frac{\sqrt{2}}{2} + \frac{\sqrt{2}}{2}i\right)$

19. Simplify  $\frac{5}{3-4i} + \frac{10}{4+3i}$

20. Simplify  $\frac{3\sqrt{2}+2\sqrt{3}i}{3\sqrt{2}-2\sqrt{3}i}$

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B.VOC(WT)& B.VOC. (IT)	II	Discrete Mathematics – II		R20WSDM201 R20ITDM201	2019-20		
Total No of Hours for Teaching – Learning		Instructional Hours for Week		Duration of Semester End Examination in Hours	Max Marks		Credits
60 Hours		Theory		3 Hours	CIA	SEE	
		4			25	75	4

**COURSE OBJECTIVES**

The aim of this course is to provide necessary information to solve problems on Algebra and their applications.

**COURSE OUTCOME**

- Understand the concept of Algebra .
- Finding Solutions in Special products , exponents , Fundamental operations ..
- Applications in classical mechanics.

***UNIT – I***

***Functions and graphs***

***Functions of two variables-rectangular co-ordinate*** system-graph of two variables-graphing the functions  $y=f(x)$

Simultaneous linear equations-linear equation of two unknowns-system of two linear equations in two unknowns-solutions by addition,subtraction,solution by substitution-system of three linear equation in three unknowns

Mathematical induction –principles of mathematical induction

***UNIT – II.***

Sets-definition of a set –sub set –set operations-Venn diagrams-algebra of sets –duality of sets –finite sets – power sets

Functions –function-real valid functions- composition of function – one-one, onto ,invertible -function recursively defined function

***UNIT – III:***

Vectors and Matrices:

Introduction-vectors-matrices-matrix addition & scalar multiplications-matrix multiplications-transpose-square matrices-invertible (non singular)matrices-inverses-determinants-elementary row operations –Gaussian elimination

## **UNIT – IV**

*Lattice –bounded lattices-distribute lattices-complements, complemented lattice*

## **UNIT –V**

Boolean algebra:

Introduction –basic definition-duality- duality principles-sum of products form of sets –sum –of-products form for boolean table ,Boolean functions logic gates-circuits-truth tables- Boolean functions

**NOTE** :Problems only on all the above concepts

### **PRESCRIBED BOOKS:**

1.Murray R-spiegal,Robert E.maver ,Schaum’s outline series –college algebra- 1956 edition

Unit-I: chap:10,12,13,15,31 of above text book

2.SEYMOUR LIPSCHUTZ: marc lipson Schaum’s outline series-discrete mathematics – second edition

Unit-II: chap-1,2,3,4;

Unit-III: chap-14,15 content &treatments as it is

### **Reference Books :**

***Bhavanari Satyanarayana*** &kuncham syam Prasad

Discrete mathematics &graph theory, printice hall of India ,learning ,New Delhi 2009.

### **Blue print :**

*Section A – One Question from each chapter of Unit – IV & Unit - V*

*- Two Questions from Unit I , Unit II & Unit III .*

*Section B - Two Questions from each Unit.*

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**MODEL QUESTION PAPER**

**SECTION -A**

**Answer any FIVE questions:**

**5x5=25M**

- 1.If  $y=5+3x-2x^2$  find the values of y corresponding to  $x=-3,-2,-1,0,1,2,3$ .
- 2.solve the equations  $3x+y-z=4$ ,  $x+y+4z=3$ ,  $9x+5y+10z=8$ .
- 3.Find the powerset P(A) of  $A =\{1,2,3,4\}$ .
- 4.If  $f:A \rightarrow R$ ,  $g:R \rightarrow R$  defined by  $f(x)=x^2+x-2$ ,  $g(x)=2x-3$  then find g of where  $A=\{1,2,3,4,5\}$ .
- 5.Find the ADJ of  $\begin{bmatrix} 4 & 5 & 6 \\ 5 & 0 & 3 \\ 2 & 4 & 7 \end{bmatrix}$ .
- 6.Define the Lattice .
- 7.Find the truth table for  $\sim(p \wedge \sim q)$ .
- 8.If  $u=(2,-3,1)$ ,  $v=(1,4,-2)$  be two vectors then compute  $(U+V) \times (U-V)$ .

**SECTION -B**

**ANSWER ALL THE QUESTIONS**

**5X10=50M**

9. A) Prove by mathematical induction that for all integers 'n'.

$$1^2 + 2^2 + 3^2 + \dots + n^2 = \frac{n(n+1)(2n+1)}{6}$$

(OR)

B). Prove by mathematical induction that for all integers 'n'.

$$\frac{1}{1.3} + \frac{1}{3.5} + \frac{1}{5.7} + \dots + \frac{1}{(2n-1)(2n+1)} = \frac{n}{2n+1}$$

10. A) If  $f:A \rightarrow B$ ,  $g:B \rightarrow C$  are two bijections then prove that  $g \circ f:A \rightarrow C$  is also a bijection.

(OR)

B) Find the formula for the inverse of  $h(x) = \frac{2x-3}{5x-7}$

11.A). Find the inverse of  $\begin{bmatrix} 1 & -2 & 2 \\ 3 & -3 & 6 \\ 1 & 1 & 7 \end{bmatrix}$  by using row operations.

(OR)

B). Show that  $\begin{vmatrix} 1 & a^2 & a^3 & a & a^2 & bc \\ 1 & b^2 & b^3 & b & b^2 & ca \\ 1 & c^2 & c^3 & c & c^2 & ab \end{vmatrix} = (a-b)(b-c)(c-a)(ab+bc+ca)$

12.A). Let 'L' be a bounded distributive lattice. Then the compliments are unique if there exists .

(OR)

B). If 'L' be a lattice then  $a \wedge b = a \Leftrightarrow a \vee b = b$ .

13. A).i) Define Boolean algebra.

ii) Describe the three basic logic gates.

(OR)

B). Show that  $(p \rightarrow q) \wedge (q \rightarrow r) \rightarrow (p \rightarrow r)$  is tautology.

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